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Technology Inc.

Internal Fluid Mechanics Division



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Analysis of Supersonic Flows using k- ϵ Model and the RPLUS code; Progress towards High Speed Combustor Analysis.

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for Workshop on Computational Turbulence Modeling

Sept. 1993



Outline

- Problem of Interest - High Speed Combustor Flow Fields
 - Parameters need to be Resolved
 - Key Problems of Interest
- k- ϵ Model and RPLUS code
 - Numerical Technique
 - Models being Tested
 - Some Results
- Summary

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Problem of Interest

- Analysis of Chemically Reacting flow inside of Supersonic RAM jet Combustors-Two Key Parameters need to be determined.
 - Mixing/Combustion Efficiency
 - Kinetic Energy Efficiency (Flow Losses)
 - Inlet, Diffuser, etc..
- In order to do get some ideas on those parameter following (Potential Loss Mechanisms) must be modeled/determined correctly.
 - Mixing, Shear,
 - Turbulence, Vorticity,
 - Shock-waves, Heat Transfer,
 - Fuel Injector Drag, Poor Wall Pressure Integral,
 - Chemical Dissociation.

from 2nd JANNAF workshop on SCRAMjet Combustor performance workshop

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Mixing and Injector Design

- At High Mach Number($M \sim 5.0 +$).
 - Doesn't mix well!
 - The Natural diffusion mechanism very INEFFECTIVE.
 - Fuel Residence Time Extremely Small- Even with Fast Fuel Such as H_2
- Geometrical Complexities
 - To induce Favorable mixing and Flame holding features
 - Back-Step/Stream Wise Vorticity/Shock-Wave Interactions
 - Unsteady Mechanism also being Envisioned as mixing enhancement
 - Kumar, Bushnell and Hussani(1987)

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Introduction of Externally Generated Mixing Enhancements

- Some External helping hand needed \Rightarrow Modeling Difficulties.
- Externally Generated Vorticity Through Sweep angle of the Ramp injector.
 - Davis(1990), Riggins and McClinton(1990), Drummond(1991).
- Multiple Transverse Injection.
 - Hartfield et. al. (1991)
- Flame holding tricks/ Back-step with Recirculation.
 - Hartfield et. al.(1991)
- Simplified analysis of these features very difficult because of limited database/understanding (Attempts are being made using CFD solutions- JANNAF Combustor Subcommittee).

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Numerical Modeling(CFD) of Combustor Flow Field

- CFD Analysis.
- Numerical Modeling=> Overall Analysis of performance => Difficult
- Overall Laminar Flow Fields with Complex Geometry/Finite Rate Chemistry has been demonstrated.
- Finite Rate Chemistry Model- Yoon and Shuen(1989)
- Multiple Grid Blocks- Moon (1991)
- Analysis of a typical Injector Configuration with Zero Equation Turbulence Model using LU Scheme(RPLUS) code- Lee(1993)

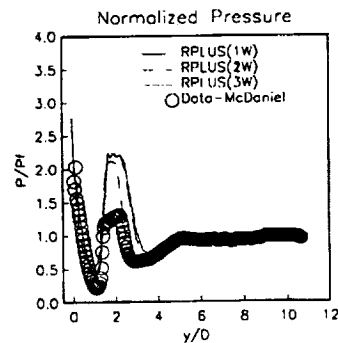
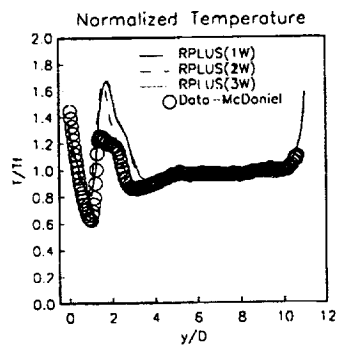
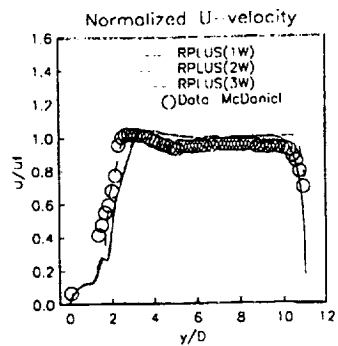
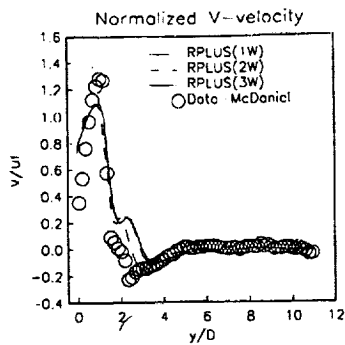
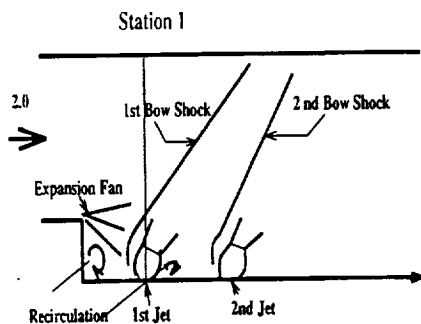
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Simple Zero Equation Turbulence model with multiple wall scaling Buleev-Inverse square rule can be used to extend model in to three-dimensional form. (Lee (1993))

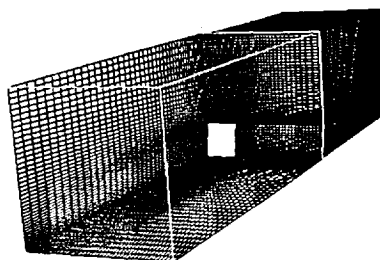
- Good News/Bad News
- Typical velocity profiles can be reasonably predicted.
- Over all combustor flow features can be reasonably predicted.
- Near-wall temperature characteristics near non-equilibrium region around the injector and separated flow were poorly predicted.
- Overall spreading behavior of shear region poorly predicted.
- Two Equation Transport Turbulence Model has the potential to ease some of these difficulties.

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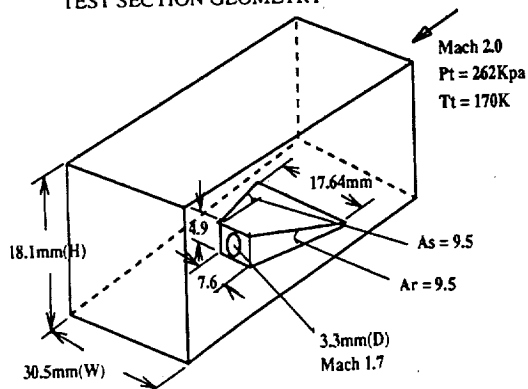


THREE-BLOCK GRID SYSTEM

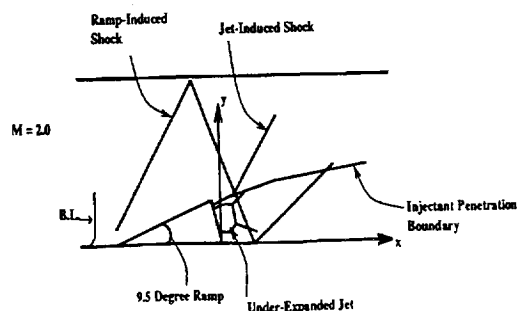
HARTFIELD ET. AL. (1990)

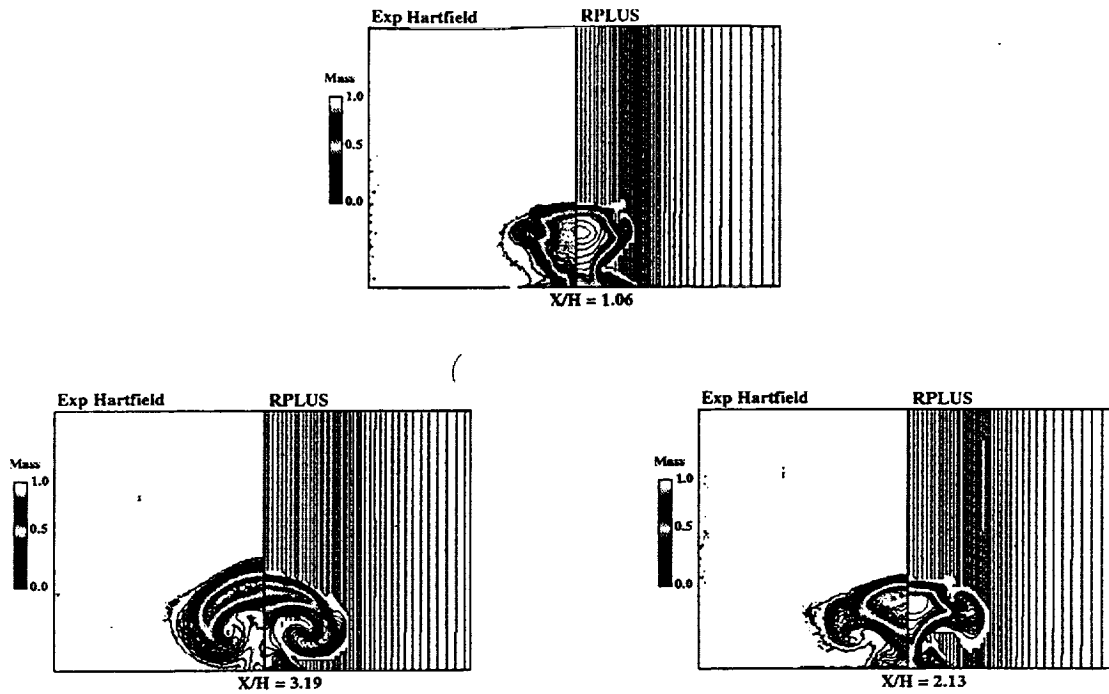


TEST SECTION GEOMETRY

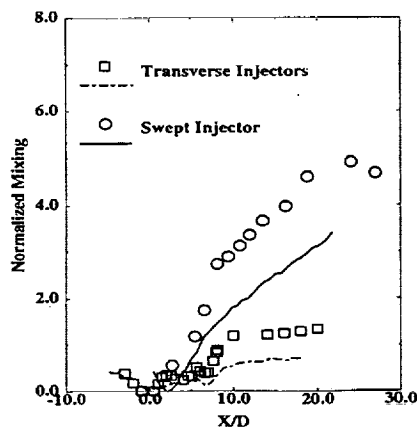


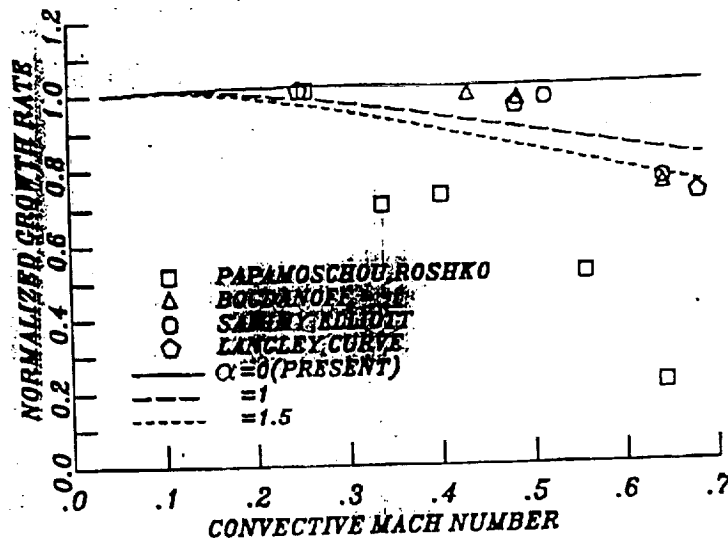
FLOW SCHEMATIC





Mixing Efficiencies





GROWTH RATE VS. COMPRESSIBILITY EFFECT

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Two Equations Transport Turbulence model are being Analyzed

- High speed turbulence models are some what Deficient (The deficiencies are well documented(Marvin(1986), Wilcox(1993))).

Effect of Compressibility

An-isotropy (Low/High Speed).

Non-Equilibrium Flow Features (Low/High Speed).

Near-Wall Flow(Low-Reynolds Number Features (Low/High Speed)).

Inflexibility of handling Complex Geometry- Invariance Principle (Low/High Speed)

Large Dependence in the Numerical Methods Used (especially elliptic Solvers).

Appropriate Initial/Boundary Conditions

Etc ...



K-ε Model-RPLUS Development

- **LU Based k-ε Model Solver-De-coupled Approach.**

Mean-Turbulence Transport Equations

LU-SSOR- Yoon and Shuen- Explicit Terms Centrally Differenced

LU-SW -Steger and Warming- Explicit Terms Upwind Differenced

k-ε Models

Convective Terms + Diffusive Terms + Source Terms = 0.0

Model Only differ in Low-Reynolds Number Character.

Models performance are being Evaluated.

Implicit Source Term Handling Strategy also Being Studied

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k-ε Turbulence Models being studied for potential used in Three Dimensional RPLUS Code.

- **Low-Reynolds Number Model plus Dilatational Terms**

Chien (1976)

Launder-Shima(1976)

Shih(1990)

Various CMOTT derivatives of k-ε Model

Realizability

Invariance

Simplified Boundary-Conditions

- Performance of the Low-Reynolds number K-ε model in low-Mach number flows have been demonstrated (Patel, Rodi and Scheuerer(1985), Steffen(1993), Launder(1992)).
- Some of the Potential Difficulties in high speed turbulence model are well documented (Marvin(1993), Coakley and Huang(1992)).

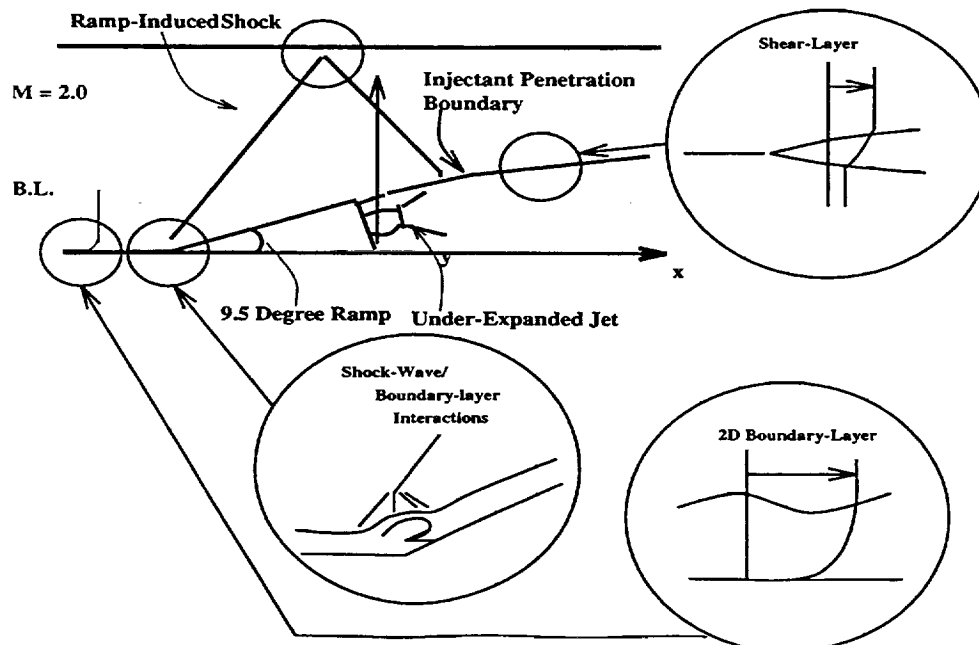
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Evaluation and Development of the RPLUS/k- ϵ Model Solver

- Various 2D-3D problems are being studied to optimize the numerical method and to Evaluate model performance in supersonic flows in context to the LU based numerical Technique.
- Simple 2D k- ϵ models are also being used to study various components of the flowfield generated by the complex combustor geometry previously shown.
- Studying the Numerical method/Model Behavior/Model Performance.
 - 2D Supersonic Turbulent Boundary-Layer- Skin Fraction/Heat transfer (NASA Ames Database).
 - 2D Supersonic Shock-Wave Boundary-Layer Interaction- Skin fraction/Heat -Transfer/ Shock-wave(A. Smits (1990's))
 - 2D Shear-Layer - Mixing (H. Lai(1993))
 - 3D Fin/Flat Plate Interaction- 3D Corner Flows-Interaction Developed through a Fin generated Shock-Waves. (D. Davis(1992))

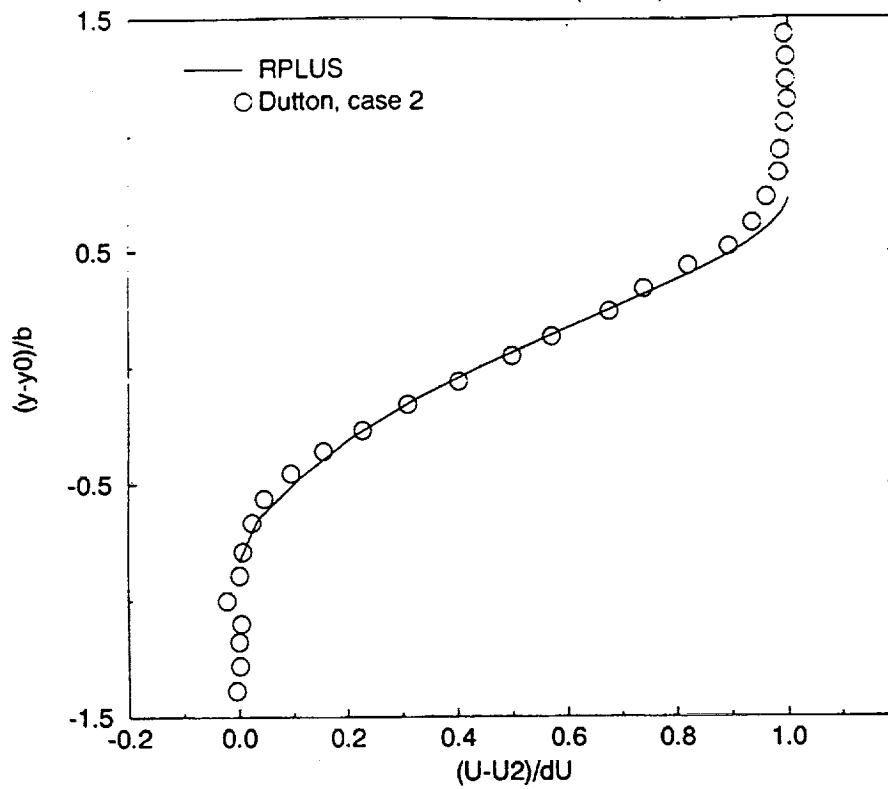
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Supersonic Mixing Layer

RPLUS vs. Dutton (case 2)



B. DUNCAN



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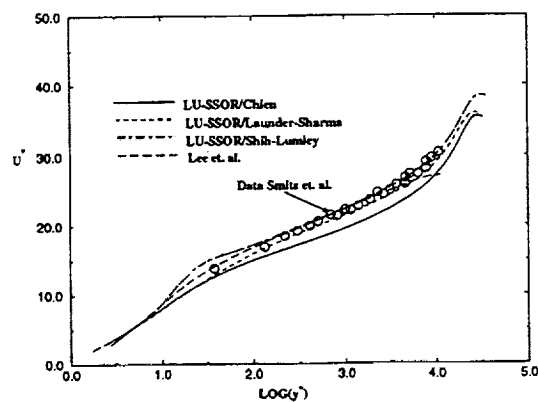


Boundary Layer

Mach 2.87

$Re/m = 6.3 \times 10^7/m$

Law of Wall Profile

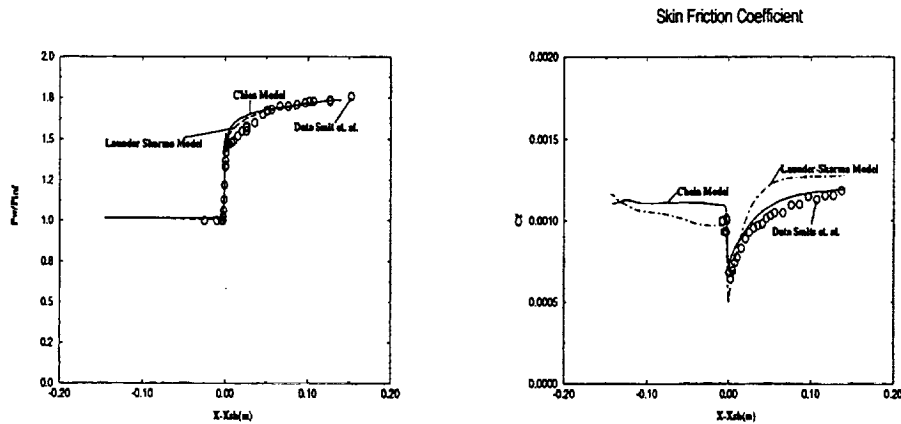




Turbulent Shock-Wave/Boundary Interactions

Mach 2.87

Ramp Angle = 8.0 degrees



Other Factors

- Optimum Numerical Strategy with in LU frame work.
- Effects of Initial condition.
- Modeling of Compressibility terms/Dilatational terms.
- Modeling of Turbulent terms in the Finite Rate Chemistry Model.
Anisotropy of Turbulence
- Effects Upstream and Down stream Influences (Inlet(K. Kapoor) and Diffuser(?)).
- Chemistry-Turbulence Model Interactions (A. Hsu-PDF).
- Numerical Robustness(A. Suresh).